

$$\begin{aligned} y = \cos(\cos(\cos x)) &\Rightarrow y' = -\sin(\cos(\cos x)) \frac{d}{dx} (\cos(\cos x)) \\ &= -\sin(\cos(\cos x)) \sin(\cos x) \sin x \end{aligned}$$