

$$\begin{aligned}\int \sec t (5 \sec t + 9 \tan t) dt &= \int (5 \sec^2 t + 9 \sec t \tan t) dt \\ &= 5 \tan t + 9 \sec t + C\end{aligned}$$