

$$f(x) = x + \frac{1}{x}, \quad D = \{x \mid x \neq 0\}; \quad g(x) = \frac{x+17}{x+2}, \quad D = \{x \mid x \neq -2\}$$

$$(a) \quad (f \circ g)(x) = f(g(x)) = f\left(\frac{x+17}{x+2}\right) = \frac{x+17}{x+2} + \frac{1}{\frac{x+17}{x+2}} = \frac{x+17}{x+2} + \frac{x+2}{x+17}$$

Since  $g(x)$  is not defined for  $x = -2$  and  $f(g(x))$  is not defined for  $x = -17$  and  $x = -2$ , the domain of  $(f \circ g)(x)$  is  $D = \{x \mid x \neq -17, -2\}$ .

$$(b) \quad (g \circ f)(x) = g(f(x)) = g\left(x + \frac{1}{x}\right) = \frac{\left(x + \frac{1}{x}\right) + 17}{\left(x + \frac{1}{x}\right) + 2} = \frac{x^2 + 17x + 1}{x^2 + 2x + 1}$$

Since  $f(x)$  is not defined for  $x = 0$  and  $g(f(x))$  is not defined for  $x = -1$ , the domain of  $(g \circ f)(x)$  is  $D = \{x \mid x \neq -1, 0\}$ .

$$(c) \quad (f \circ f)(x) = f(f(x)) = f\left(x + \frac{1}{x}\right) = \left(x + \frac{1}{x}\right) + \frac{1}{x + \frac{1}{x}} = x + \frac{1}{x} + \frac{x}{x^2 + 1}, \quad D = \{x \mid x \neq 0\}$$

$$(d) \quad (g \circ g)(x) = g(g(x)) = g\left(\frac{x+17}{x+2}\right) = \frac{\frac{x+17}{x+2} + 17}{\frac{x+17}{x+2} + 2} = \frac{6x+17}{x+7}$$

Since  $g(x)$  is not defined for  $x = -2$  and  $g(g(x))$  is not defined for  $x = -7$ , the domain of  $(g \circ g)(x)$  is  $D = \{x \mid x \neq -2, -7\}$ .